

Department of Mathematics
Pattamundai College, Pattamundai
6th Semester
Linear Programming
Core - 14
Section - A

1. a) What are the three components of linear programming problem?
- b) Write the different steps in order to form the mathematical formulation of LPP.
- c) Which of the following is not associated with an LPP ?
- i) Proportionality (ii) Uncertainty (iii) Additivity (iv) Divisibility
- d) What is the restriction for a constraint in a LPP ?
- e) What is the meaning of minimization of objective function in LPP ?
- f) Why non negative condition is an important component of LPP ?
- g) Variables can be unrestricted in the context of an LPP (True / False)
- h) The graphic approach to an LPP is applicable when the number of decision variables are more than the number of constraints (True / False)
- i) A feasible solution to an LPP must satisfy all the problem's constraints simultaneously. (True/False)
- j) It is not possible to obtain feasible solution of an LPP by graphical method (True/False)
- k) If two constraints do not intersect in the positive quadrant of the graph then the solution is infeasible (T/F)
- l) Using graphic method, the optimum solution of the LPP of maximizing $z = 10x + 15y$ subject to $2x + y \leq 26$, $x + 2y \leq 28$, $y - x \leq 5$, and $x \geq 0$, $y \geq 0$ is obtained as _____
- m) An iso-cost line cannot be parallel to the line of any constraint. (True/False)
- n) Given a system of m simultaneous linear equations in n unknowns ($m < n$), the number of basic variables will be _____
- o) For maximization linear programming problem, the simplex method is terminated when all the net evaluations are negative (True / False)
- p) Solution by simplex method requires that an LPP should have at least one non negative values in the right hand side of the constraints (True / False)

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- q) What is the role of artificial variables in simplex method ?
 - r) For maximization LPP, the objective function coefficient for an artificial variable is _____
 - s) If an optimum solution is degenerate then what happened ?
 - t) When we solve a system of simultaneous linear equations by using Two-phase simplex method the values of decision variables may be positive and / or negative. (True/False)
 - u) If dual has an unbounded solution, primal has _____
 - v) Dual simplex method is applicable to these LPP's that state with an infeasible but optimum solution (True/False)
 - w) All scarce resources have marginal profitability equal to zero (True/False)
 - x) If the number of primal variables is very small and the number of constraints is very large, then it is more efficient to solve the dual rather than the primal problem . (True/False)
 - y) The transportation problem deals with the transportation of a single product from several sources to a destination (True/False)
 - z) The transportation problem is balanced, if total demand equals total supply irrespective of the number of sources and destinations. (True/False)
2. a) The solution to a transportation problem with m-sources and n-destinations is feasible, if the number of allocations are _____
- b) While solving a transportation problem the occurrence of degeneracy means the solution so obtained is not feasible. (True / False)
 - c) In vogel's approximation method the cost difference indicate the penalties for not using the respective least cost - routes (True/ False)
 - d) The initial solution of a T.P. Obtained by VAM would invariably be very near to optimum solution (True/False)
 - e) The dummy source or distention in a T.P. is introduced to satisfy rim conditions. (True/False)
 - f) Any of the $m+n-1$ number of occupied cells would allow determining whether a given solution is optimum or not ? (True/False)

- g) For a transshipment problem an m source, n destination transportation problem, when written as a transshipment problem would have $m+n$ sources and n destinations. (True/False)
- h) The assignment problem is a special case of transportation problem in which number of Origins equal to the number of _____.
- i) Why an assignment problem is consider as a particular case of transportation problem .
- j) If there are n workers and n jobs, there would be _____ solutions.
- k) In an assignment problem involving four workers and three jobs, total number of assignments possible are _____
- l) Which method is used for solving an assignment problem ?
- m) An assignment problem can be solved by transportation method and simplex method (True/False)
- n) For a salesman, who has to visit n cities, _____ number of ways he can made his tour plan.
- o) Define 'A game is said to be fair'
- p) When maximin and minimax values of the game are same then there is a saddle point. (True/False)
- q) A mixed strategy game can be solved by _____ methods.
- r) The size of the pay-off matrix of a game can be reduced by using the principles of _____
- s) Game which involve more than two players are called _____ games.
- t) If the pay- off matrix of a game is transposed, saddle point of the game of exists changes. (T/F)
- u) In a two person zero-sum game player A's strategy is determined on the basis of maximum Griterion, Where as the basis of maximum criterion, where as player B's on the basis of minimax criterion / (T/F)
- v) In a two person zero sum game strategies of the players are played in random order in the ratio determined by the optimum mix. (True/ False)
- w) In a two person zero sum game, Row/column player is said to dominate the other player if he has more strategies to play (True/False)

Section - B

- 1.a) Explain the linear programming problem giving two examples ?
- b) What are the components of linear programming model ?

- c) Give the general form of a basic model of linear programming ?
- d) State any two applications of linear programming ?
- e) Explain the advantages of linear programming and its limitations.
- f) Explain the major characteristics of a linear programming problem.
- g) What are the major assumptions and limitations of linear programming ?
- h) "Linear programming has no real application" Do you agree ? Discuss.
- i) "Linear programming is useful Management science Technique, but it has some limitations". Discuss it and give appropriate examples.
- j) Write down the standard form of a LPP.
- k) What is feasible region ? Is it necessary that it should always be a convex set ?
- l) Illustrate graphically the following special cases of linear programming problems :
 - i) Multiple optimal solution.
 - ii) No feasible solution.
 - iii) Unbounded solution.
- m) Define slack and surplus variable in LPP.
- n) State the general linear programming problem in
 - i) Standard form
 - ii) Canonical form
- o) With the help of suitable sketches, define convex, non convex and infeasible region in relation to the graphical solution of a linear programming problem.
- p) Define the following terms
 - i) Basic variable
 - ii) Basic solution
 - iii) Basic feasible solution
 - iv) Degenerate basic solution.

q) Differentiate between basic and non-basic variables . What is an artificial variable and why should it be introduced into a solution.

r) What are the two conditions to be satisfied to perform optimality test ?

s) While solving a linear programming problem.

Maximize $z = (x \text{ st } Ax = b, x \geq 0$: what indicates the following ?

i) Unique optimal solution

ii) Presence of redundant constraints.

iii) No feasible solution.

t) How do you conclude that a LPP has an infeasible solution while using simplex method ?

u) How do you identify multiple solution in a linear programming problem ?

v) What do you mean by the two phase method for solving a given LPP ?

w) Define dual . Give any two relationships between a primal and a dual ?

x) State the duality theorem.

y) State the general rules for forming a dual LPP from its dual.

z) Write short note on 'Complementary slackness'

2.a) Give the application of duality theory

b) What is transportation problem ?

c) What is a balanced transportation problem ? What are its applications ?

d) Give a brief outline of the procedure for solving a transportation problem.

e) Explain the following in the context of T.P.

i) Stepping stone method

ii) Degenerate Transportation problem

iii) Modified distribution method.

f) What is an assignment problem ?

g) Give two applications of assignment problem in health care administration.

- h) Give the mathematical formulation of an assignment problem.
- i) Explain the difference between a transportation problem and an assignment problems.
- j) "An assignment problem is a special case of a transportation problem". Explain
- k) Explain Hungarian algorithm.
- l) Can there be multiple optimal solutions to an assignment problem ? How would you identify the existence of multiple solutions, if any ?
- m) How does travelling salesman problem differ from an assignment model ?
- n) Write a short note on Travelling salesman problem.
- o) What is game Theory ?
- p) Explain advantages and disadvantages of game Theory ?
- q) Define the term 'strategy' and 'optimal strategy' with reference to game theory.
- r) Explain the concept of value of a game.
- s) Discuss dominance with reference to game theory.
- t) What are the major applications of game theory ?
- u) Define saddle point. Is it necessary that a game should always possess a saddle point ?

Section - C

1. a) An animal feed company must produce 200lbs of a mixture containing the ingredients x_1 and x_2 . x_1 costs Rs 3 per lb and x_2 costs Rs 8 per lb. Not more than 80lbs of x_1 can be used and minimum quantity to be used for x_2 is 60lbs. Find how much of each ingredient should be used if the company wants to minimize the cost. Formulate.
- b) Use graphical method to solve the LPP Maximize $z = 2x_1 + 4x_2$ subject to the constraints :
 $x_1 + 2x_2 \leq 5$, $x_1 + x_2 \leq 4$: and $x_1, x_2 \geq 0$
- c) Consider the following LPP :
 Maximize $Z = 3x_1 + 7x_2$ subject to the constraints :
 $4x_1 + 5x_2 \leq 20$, $2x_1 + x_2 \leq 6$, $2x_1 \geq 7$, $2x_2 \leq 7$:
 $x_1 \geq 0$, $x_2 \geq 0$.

Demonstrate whether it is possible to get a solution to the above LPP.

- d) Reduce the following LPP to its standard form:

Maximize $z = x_1 - 3x_2$ subject to the constraints :

$$-x_1 + 2x_2 \leq 15, x_1 + 3x_2 = 10$$

x_1 and x_2 unrestricted in sign

- e) Show that the following system of linear equations has a degenerate solution :

$$2x_1 + x_2 - x_3 = 2$$

$$3x_1 + 2x_2 + x_3 = 3$$

- f) Find all the basic feasible solutions of the equations :

$$2x_1 + 6x_2 + 2x_3 + x_4 = 3$$

$$6x_1 + 4x_2 + 4x_3 + 6x_4 = 2$$

- g) Let $x_1 = 2$, $x_2 = 4$ and $x_3 = 1$ be a feasible solution to the system of equations

$$2x_1 - x_2 + 2x_3 = 2$$

$$x_1 + 4x_2 = 18$$

Reduce the given feasible solution to a basic feasible solution.

- h) Use simplex method to solve the LPP

Maximize $Z = 4x_1 + 5x_2 + 9x_3 + 11x_4$ subject to the constraints :

$$x_1 + x_2 + x_3 + x_4 \leq 15$$

$$7x_1 + 5x_2 + 3x_3 + 2x_4 \leq 120$$

$$3x_1 + 5x_2 + 10x_3 + 15x_4 \leq 100$$

$$x_1, x_2, x_3, x_4 \geq 0$$

- i) Use two phase simplex method to solve

Maximize $z = 5x_1 - 4x_2 + 3x_3$

s.t. the constraints :

$$2x_1 + x_2 - 6x_3 = 20, 6x_1 + 5x_2 + 10x_3 \leq 76$$

$$8x_1 - 3x_2 + 6x_3 \leq 50, x_1, x_2, x_3 \geq 0$$

- j) Solve the following LPP

Maximize $z = 2x_1 + 3x_2 + 10x_3$ s.t. the constraints :

$$x_1 + 2x_2 = 0, x_2 + x_3 = 1 : x_1, x_2, x_3 \geq 0$$

k) Solve the following system of simultaneous linear equations by using the simplex method :

$$x_1 + x_2 = 1, 2x_1 + x_2 = 3$$

l) Formulate the dual of the following LPP :

Maximize $z = 10x_1 + 8x_2$ s.t. the constraints :

$$x_1 + 2x_2 \geq 5, 2x_1 - x_2 \geq 12, x_1 + 3x_2 \geq 4,$$

$$x_1 \geq 0 \text{ and } x_2 \text{ is unrestricted.}$$

m) Use duality to solve the following LPP :

Maximize $z = 2x_1 + x_2$ s.t. the constraints :

$$x_1 + 2x_2 \leq 10, x_1 + x_2 \leq 6, x_1 - x_2 \leq 2,$$

$$x_1 - 2x_2 \leq 1 : x_1, x_2 \geq 0$$

n) Use dual simplex method to solve the following LPP :

Minimize $Z = 3x_1 + x_2$ s.t. the constraints :

$$x_1 + x_2 \geq 1, 2x_1 + 3x_2 \geq 2, x_1, x_2 \geq 0$$

o) Use Vogel's Approximate method to obtain an initial basic feasible solution of the transportation problem :

	D	E	F	G	Available
A	11	13	17	14	250
B	16	18	14	10	300
C	21	24	13	10	400
Demand	200	225	275	250	

p) Given $x_{13} = 50$ units, $x_{14} = 20$ units, $x_{21} = 55$ units, $x_{31} = 30$ units, $x_{32} = 35$ units only $x_{34} = 25$ units. Is it an optimal solution to the transportation problem :

	Available units				
	6	1	9	3	70
	11	5	2	8	55
	10	12	4	7	90
Required units :	85	35	50	45	

If not, modify it to obtain a better feasible solution.

q) Consider the problem of assigning five jobs to five persons. The assignment costs are given as follows :

		Job				
		1	2	3	4	5
person	A	8	4	2	6	1
	B	0	9	5	5	4
	C	3	8	9	2	6
	D	4	3	1	0	3
	E	9	5	8	9	5

Determine the optimum assignment schedule.

r) Solve the game whose payoff matrix is giving by ,

		Player A		
		A ₁	A ₂	A ₃
Player B	B ₁	1	3	1
	B ₂	0	-4	-3
	B ₃	1	5	-1

s) Solve the following 2-person zero-sum game :

i)

		Player B		
Player A		15	2	3
		6	5	7
		-7	4	0

ii)

		Player B		
Player A		-2	12	-4
		1	4	8
		-5	2	3

t) Determine the optimum strategies and the value of the game from the following 2x5 pay off matrix game for x :

		Y				
x		6	3	-1	0	-3
		3	2	-4	2	-1

u) Consider the following 2x2 game :

$$\begin{bmatrix} 4 & 7 \\ 6 & 5 \end{bmatrix}$$

i) Does it has a saddle point ?

ii) Is it correct to state that the value of game G, will satisfy $5 < G < 6$?

iii) Determine the frequency of optimum strategies by matrix oddment method and find the value of game .

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